X-ray Diagnostics*

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^{*} This work performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344. Also supported by LDRDs 08-ERI-002, 08-LW-004, SEGRF SFB162, the Alexander-von-Humboldt foundation and the National Laboratory User Facility program.

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Accurate diagnostics of the physics of Warm Dense Matter has been developed applying X-ray Thomson scattering

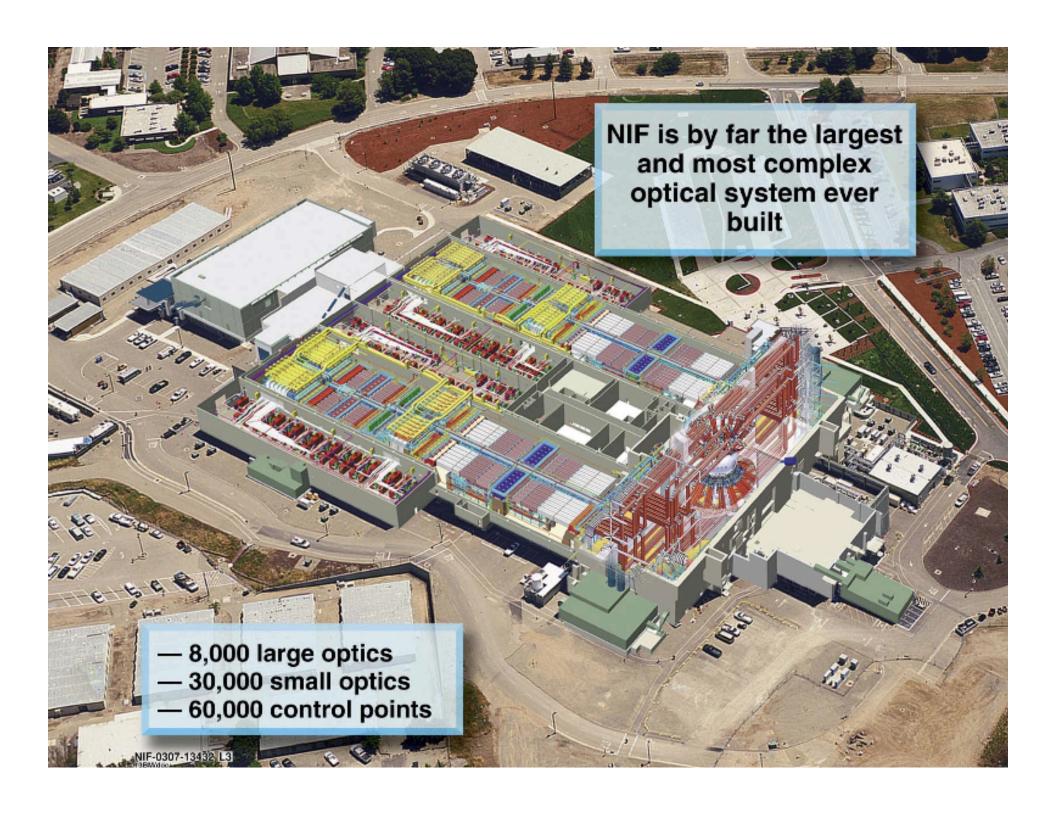
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- Introduction
 - X-ray Thomson scattering from solid density plasmas
- Proof of principle experiments
 - Backscattering experiment
 - Compton scattering in dense plasmas
 - Accurate temperature diagnostics
 - Forward scattering experiment
 - First observation of Plasmons in Warm Dense Matter
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 - Importance of collisions
- Compressed Matter
 - Compressibility and adiabat
 - Structure Factors
 - Coalescing shocks
- Outlook and Conclusions



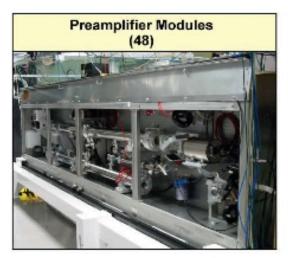




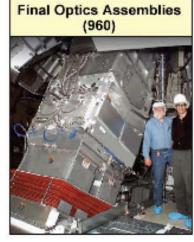


6,206 line replaceable units (LRUs) are being assembled, installed, and commissioned to complete NIF

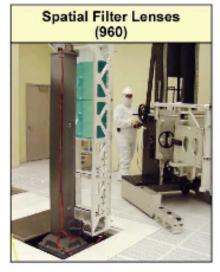


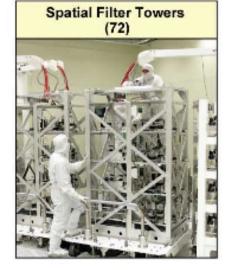








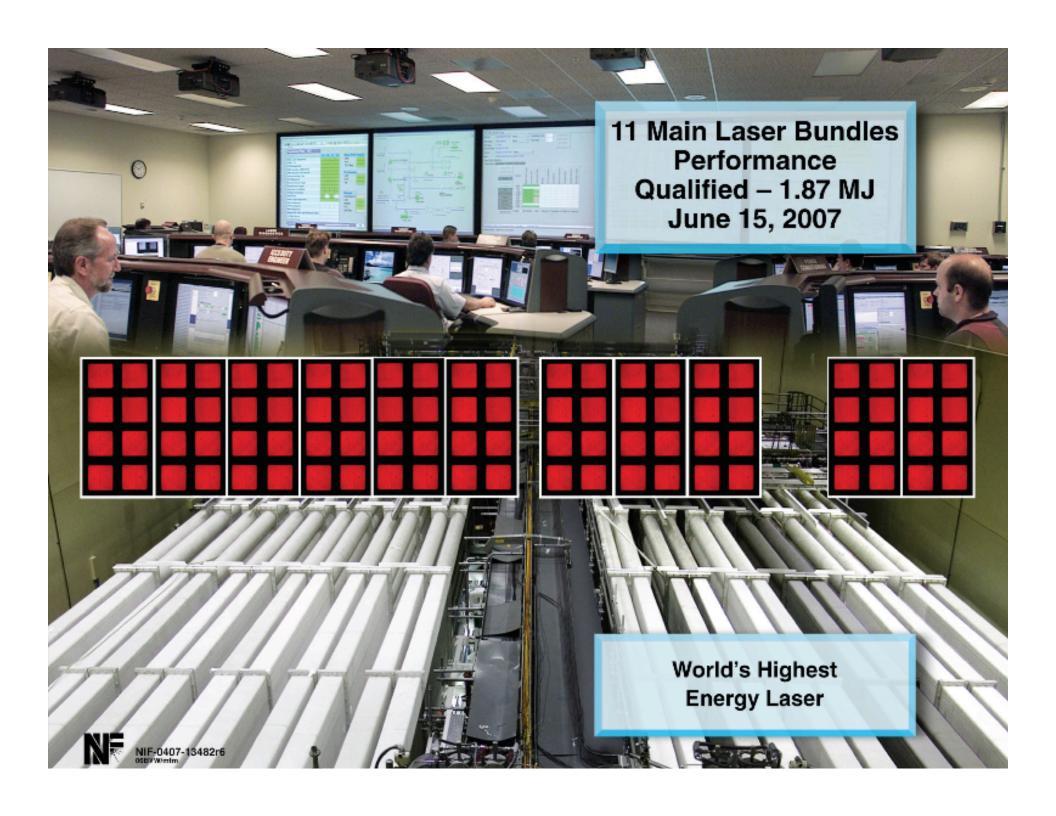


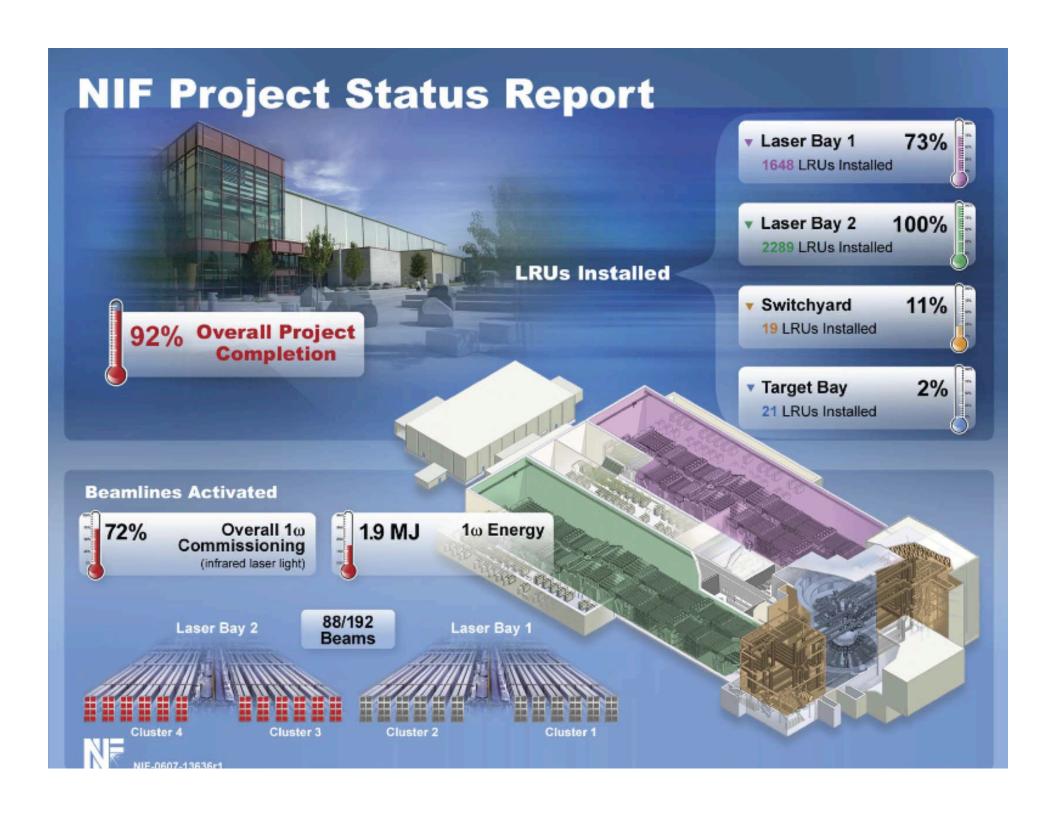




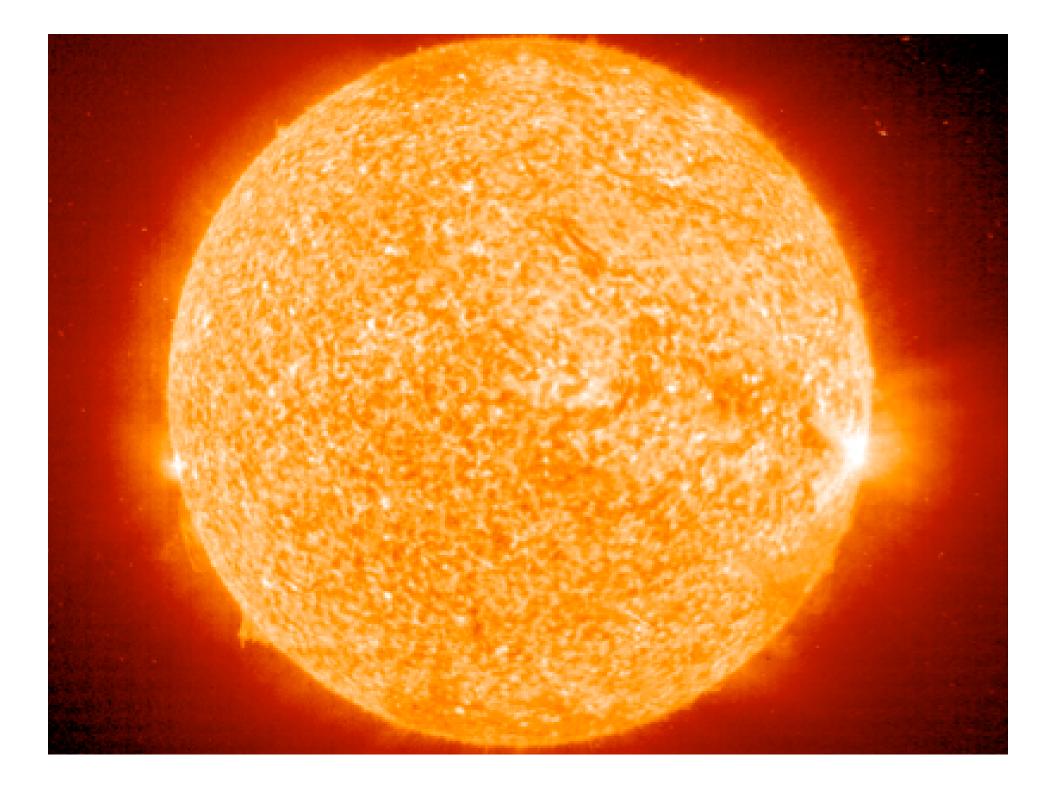






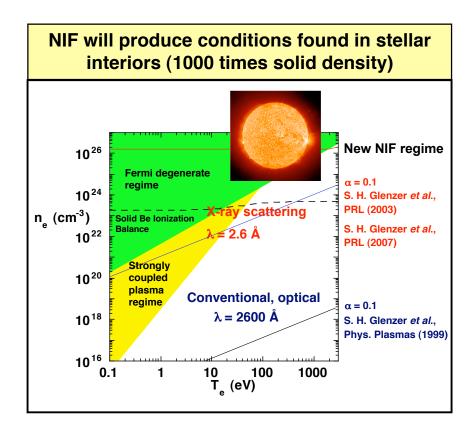






NIF will produce new states of matter that can be directly measured with x-ray scattering





Penetrating x rays are being applied to study the physical properties of dense matter



Wilhelm Röntgen, first Novel prize in physics, 1901



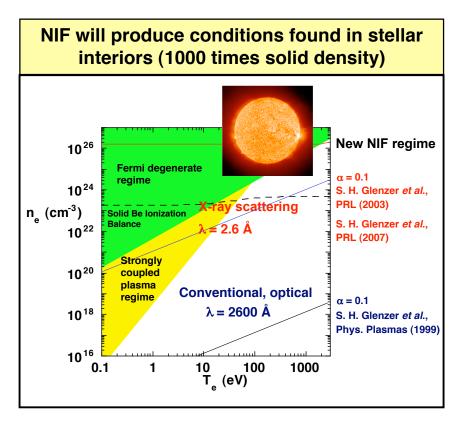
Röntgen started to take the first radiographs of his wife's hand

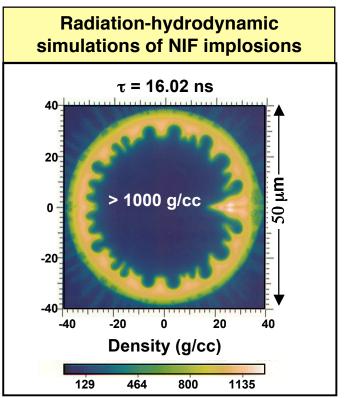


- Time-resolved X-ray backlighting/ imaging will provide velocity [engineering and laser science problem]
- X-ray scattering will determine the physics of dense matter: structure and properties

NIF will produce new states of matter that can be directly measured with x-ray scattering



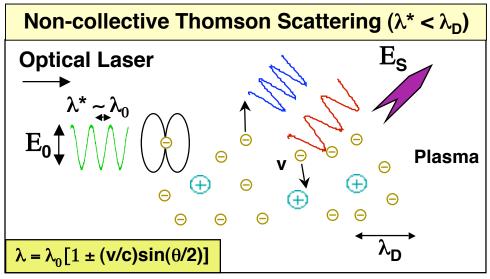




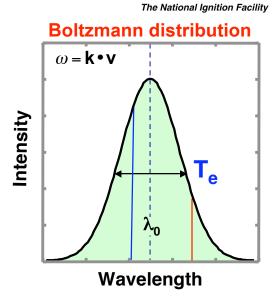
- X-ray scattering provides temperature and density
- Need intense high-energy radiation to penetrate through the capsule and to avoid bremsstrahlung emission
- Determine compression and adiabat of dense plasmas on NIF

From optical 'Thomson scattering' to x-ray 'Compton' Scattering





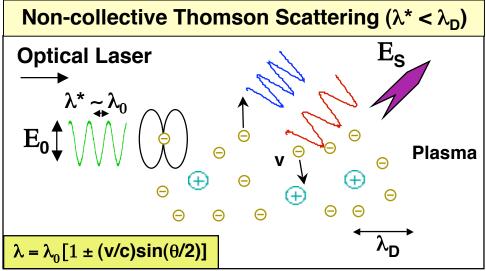
Scattering on free electrons



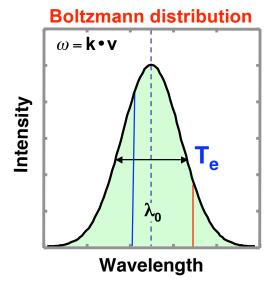
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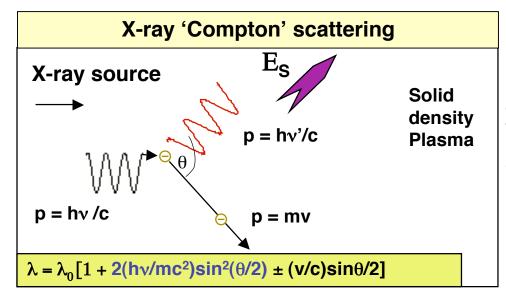




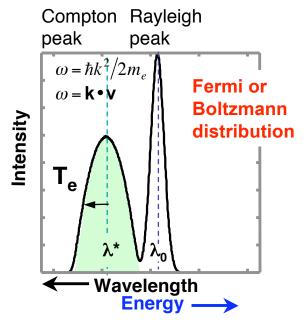


Scattering on free electrons





Scattering on free and weakly bound electrons

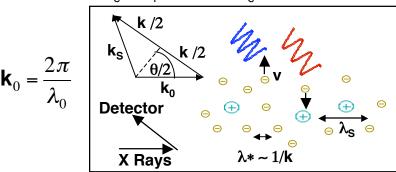


Example of Doppler and Compton shift, and dependence of shape on plasma conditions



Solid density plasma with:

$$T_e = T_i = 12 \text{ eV}; n_e = 3 \text{ x } 10^{23} \text{ cm}^{-3}$$



$$\mathbf{k} = 2\mathbf{k_0} \sin \theta / 2$$

$$\theta = 110^{\circ}$$
; $E_0 = 4.75 \text{ keV } \rightarrow 2.6 \text{Å}$ [Ti He- α]

$$k = 4 \times 10^{-10} \text{ m}^{-1} \rightarrow \lambda^* = 1.6 \text{ Å}$$

Compare with screening length [Debye length]:

$$\lambda_S \approx \lambda_D = 0.5 \text{Å}$$

$$\alpha = \frac{1}{k\lambda_S} = \frac{\lambda^*}{2\pi\lambda_S} \approx 0.5$$

Individual e- motion is observed

$$\omega = \Delta \omega = \frac{2\pi c}{\lambda_0} - \frac{2\pi c}{\lambda} = \mathbf{k} \cdot \mathbf{v}$$

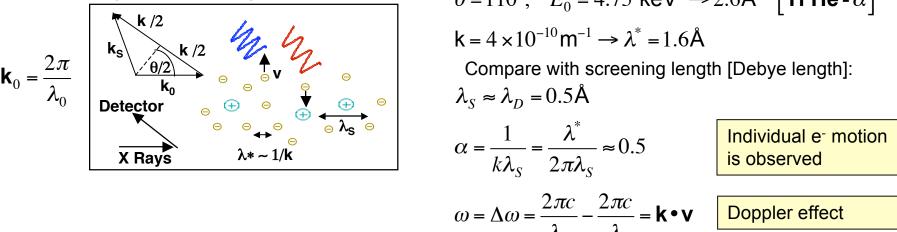
Doppler effect

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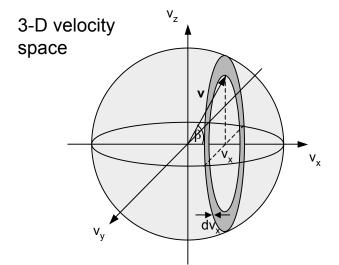
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 Doppler effect



$$f(v_x)dv_x = \int_{v_x}^{v=\infty} n(v) 2\pi \sqrt{v^2 - v_x^2} \frac{dv}{\sin \beta} dv_x$$

$$use: v_x = v \cos \beta; v_F = \sqrt{2\varepsilon_F/m_e}$$

$$f\left(\frac{v_x}{v_F}\right) = \int_0^{2\pi} \frac{\left(v_x/v_F \cos \beta\right)^2 \tan \beta d\beta}{\exp\left(\left(\left(v_x/v_F \cos \beta\right)^2 - 1 + \left(\pi^2/12\right)\left(T_e/\varepsilon_F\right)^2\right) / \left(T_e/\varepsilon_F\right)\right) + 1}$$

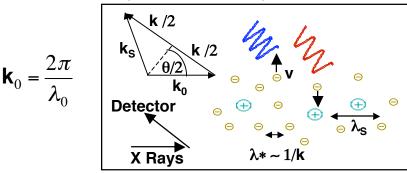
$$\varepsilon_F = \frac{\hbar^2}{2m_e} \left(3\pi^2 n_e\right)^{\frac{2}{3}} = 17\text{eV}; \quad f(E) = \frac{1}{\exp\left((E - \varepsilon_F)/T_e\right) + 1}$$

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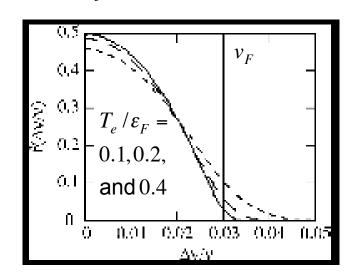


Solid density plasma with:

$$T_e = T_i = 12 \text{ eV}; n_e = 3 \text{ x } 10^{23} \text{ cm}^{-3}$$



$$E_C = \frac{\hbar^2 k^2}{2m} = 58\text{eV}$$



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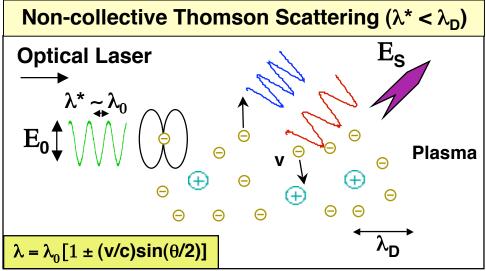
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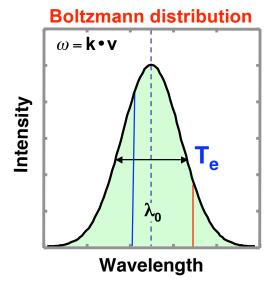
From optical 'Thomson scattering' to x-ray 'Compton' Scattering

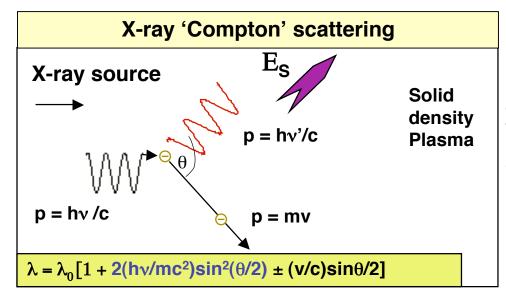




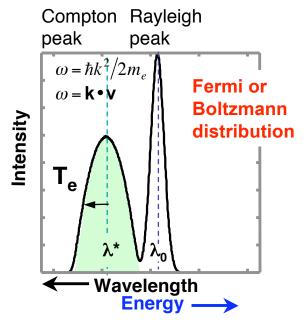


Scattering on free electrons





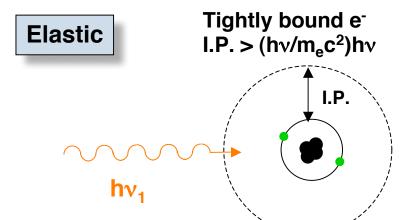
Scattering on free and weakly bound electrons



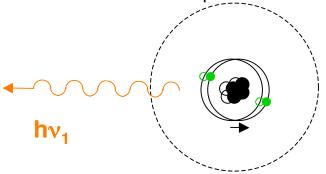
X-ray scattering divided between elastic (Rayleigh) and inelastic (free plus weakly bound) components

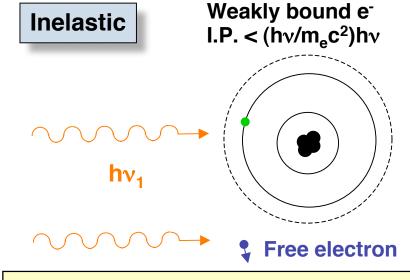


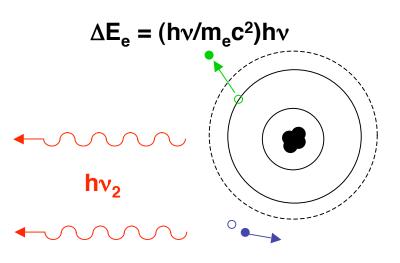
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Tightly bound electrons give Rayleigh peak and correction to the Compton shift







O. L. Landen et al., JQSRT 71, 465 (2001):

Max. θ : \longrightarrow max. Compton shift

 $hv_2 = hv_1 - (hv/m_ec^2)hv(1-cos\theta)$ (Compton) $\pm 2hv(v_e/c)sin\theta/2$ (Doppler)

max. Doppler broad.

X-ray Thomson scattering has been shown to accurately characterize dense compressed matter

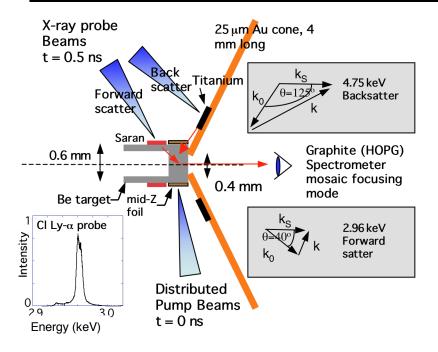


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X-ray "Thomson' scattering in warm solid density matter was first demonstrated on beryllium at the Omega laser

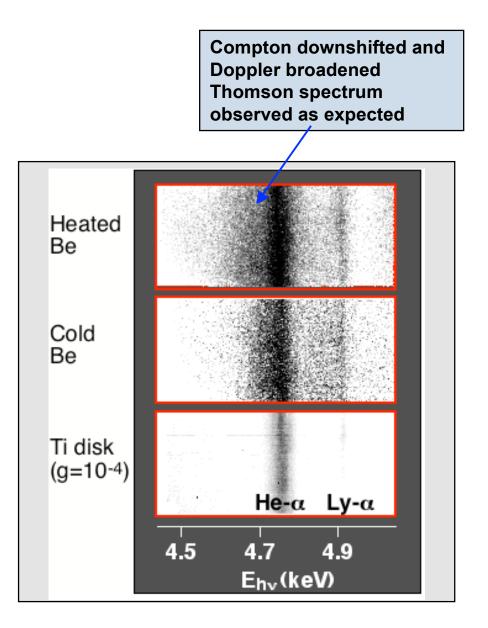


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 T_e broadening was predicted in 1928: Chandrasekhar: "scattering will not be influenced by ranges of temperatures available in the laboratory" Proc R.S. A 125, 37 (1929)

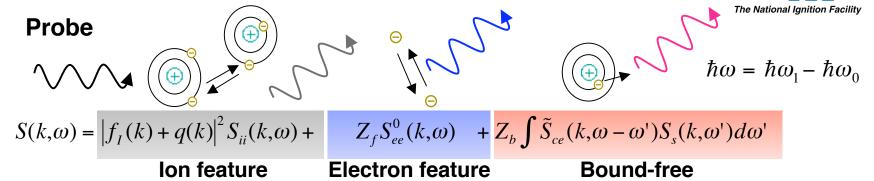
S. H. Glenzer et al., Phys. Rev. Lett. 90, 175002 (2003).

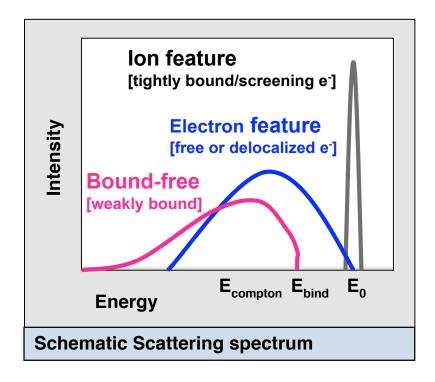


Experiment

The theoretical form factor for x-ray scattering provides reliable plasma parameter for back scatter experiments







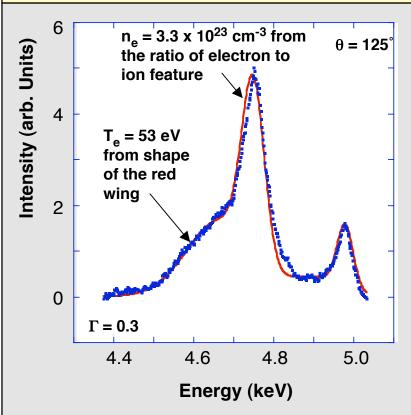
- Free or delocalized electrons result in the Compton down-shifted line, Z_f S_{ee} (k,ω)
- Bound-free contribution also results into down-shifted spectrum
- $Z_b S_{ce} (k,\omega)$
- The momentum of bound e⁻ causes broadening
- The ion feature describes elastic scattering S_{ii}(k,ω)
- In backscatter: theoretical approximations agree



X-ray scattering provides accurate temperature measurements in solid-density Be plasmas



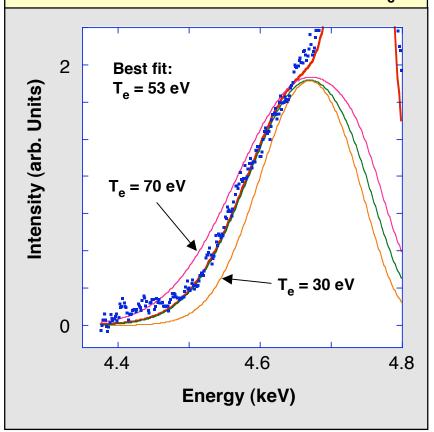
X-ray scattering spectra provide accurate data on $T_{\rm e}$ and $n_{\rm e}$



From the theoretical fit to the data:

 T_e = 53 eV and Z_{free} = 3.1 corresponding to n_e = 3.8 x 10^{23} cm⁻³

Comparison of experimental data with theoretical calculations for various T_e



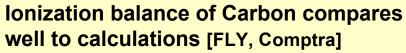
A sensitivity analysis shows that we can measure T_e with an error bar of ~15%

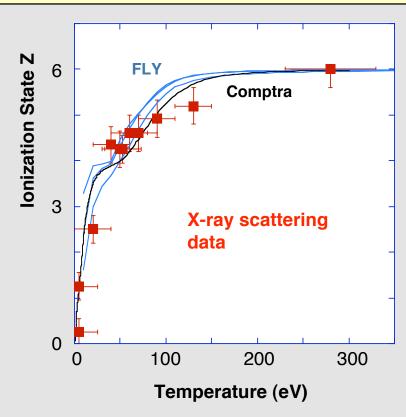


X-ray scattering application: test of ionization balance models in dense plasmas



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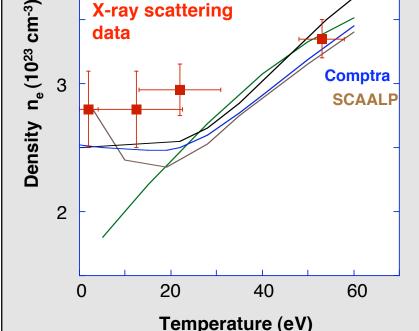




ACTEX **LASNEX** X-ray scattering data

Electron density can be inferred from

the Ionization balance of Beryllium



X-ray scattering has been successfully applied in different targets varying in density from $10^{21} < n_a < 10^{23}$ cm⁻³

Be and Z = 2.5: $n_e = 3 \times 10^{23} \text{ cm}^{-3}$

In isochorically heated matter we have:

 $n_o = 6 \times 10^{23}$ Z/A ρ cm-3 and with $\rho = 1.85$ for

Gregori et al, JQSRT (2006)

Glenzer et al, PoP (2003)

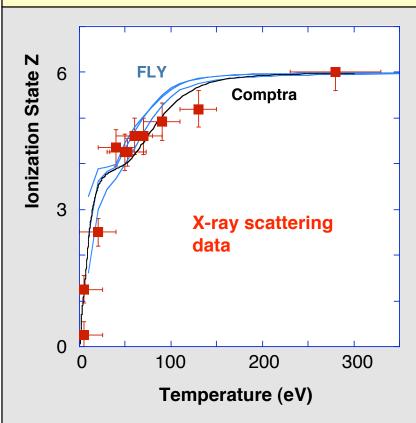


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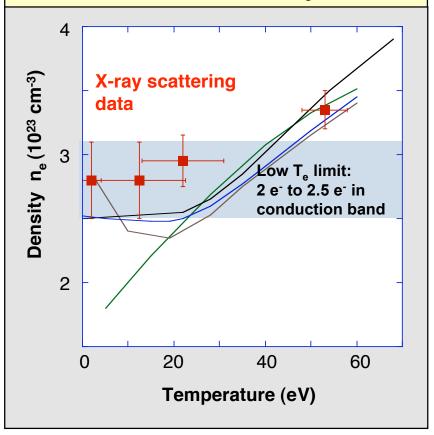
Ionization balance of Carbon compares well to calculations [FLY, Comptra]



X-ray scattering has been successfully applied in different targets varying in density from $10^{21} < n_e < 10^{23} \text{ cm}^{-3}$

Gregori et al, JQSRT (2006)

Electron density can be inferred from the Ionization balance of Beryllium



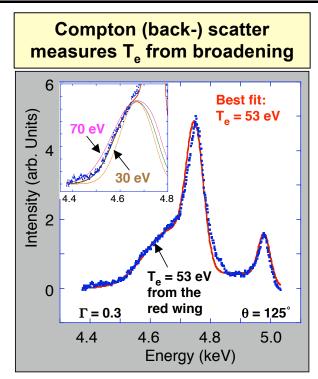
In isochorically heated matter we have: n_e = 6 x 10²³ Z/A ρ cm-3 and with ρ = 1.85 for Be and Z = 2.5: n_e = 3 x 10²³ cm⁻³

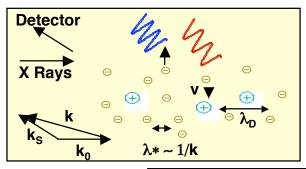
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Experiment

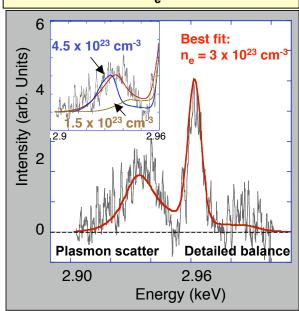
Back- and forward scatter have been demonstrated on Omega accurately characterizing solid-density plasmas

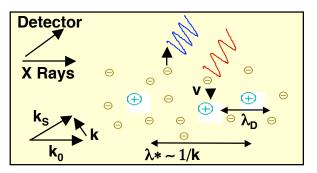






Forward scatter on Plasmons measures n_e from shift

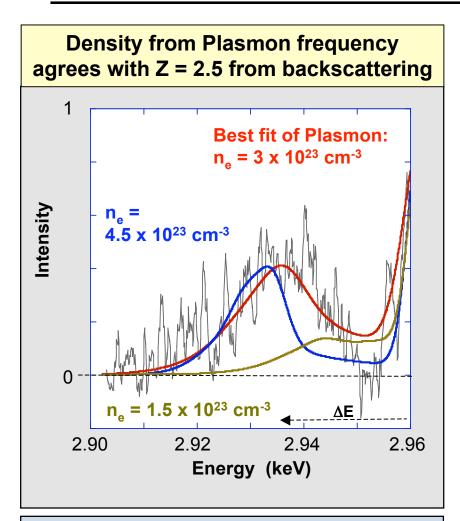




$$\lambda^* > \lambda_S$$
 or $\alpha = \frac{\lambda^*}{\lambda_S} = \frac{k^{-1}}{\lambda_S} = \frac{\lambda_0}{4\pi \lambda_S \sin(\theta/2)} > 1$

The plasmon frequency provides a robust measure of the density





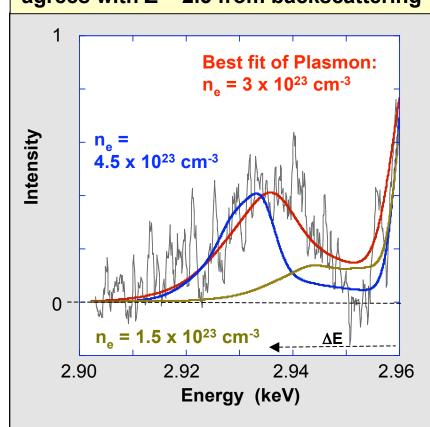
Sensitivity analysis shows error bar in electron density of ~25% [Reducing noise will improve this value]

Experiment

The plasmon frequency provides a robust measure of the density

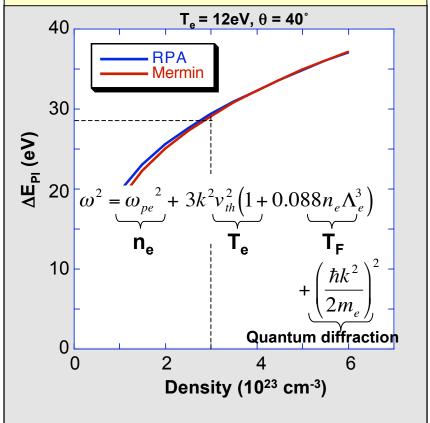






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Plasmon dispersion relation indicates accurate density measurement

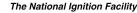


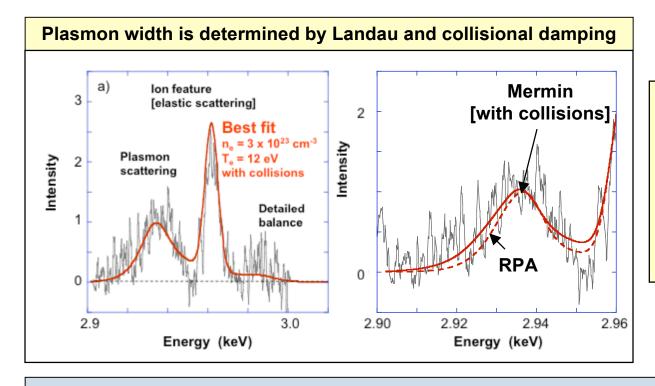
- Leading term is density sensitive (ω_{ne})
- Diffraction is determined by θ and E_0
- Thermal correction (T_e) is of order E_C

Collisions

Plasmon spectra have been shown to be sensitive to collisions, a fact that can be used to measure conductivity







Dashed curved is collision-less theory: Random Phase Approximation

Solid curves use Mermin theory with collisions, ν_{ei} , in Born approximation

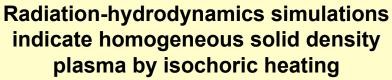
- Here, collisions provide a correction to the width [important to obtain fit with proper T_evalues
- To accurately determine n_{ei} and conductivity we will implement improvements access the collision dominated regime
 - FEL experiment [A. Höll et al, HEDP 3 (2007)]
 - New experiments with lower x-ray energy on Omega

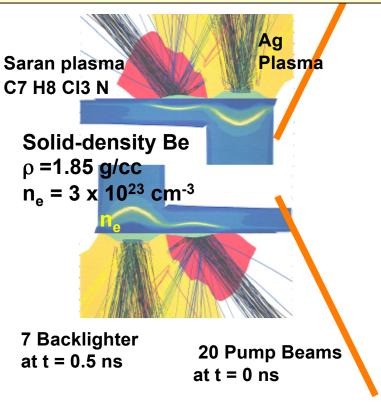
Experiment

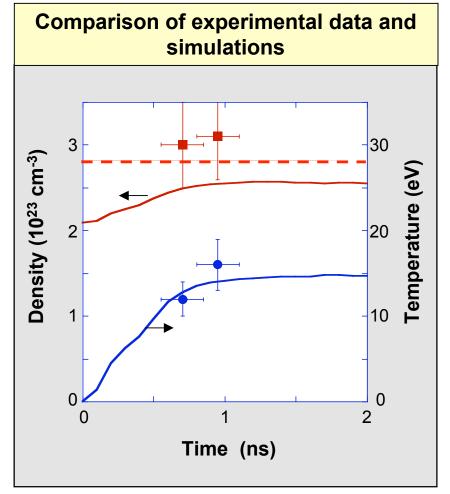
Forward scattering provides n_e and T_e data consistent with previous backscatter measurements and simulations

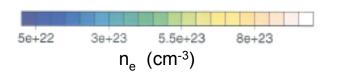


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X-ray Thomson scattering has been shown to accurately characterize dense compressed matter



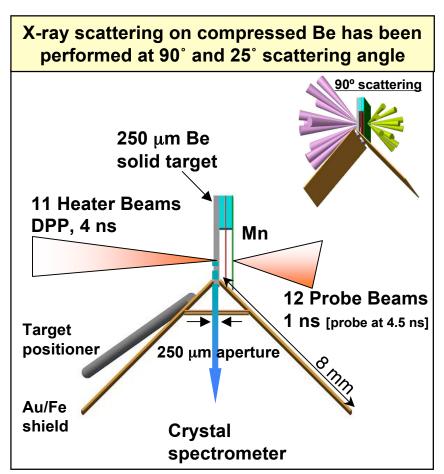
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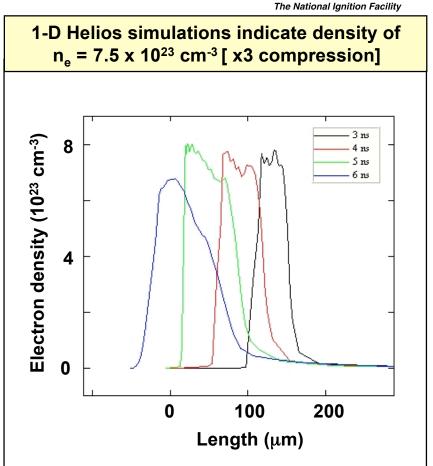
Compressed Matter



Compressed Be at 30 Mbar has been characterized with x-ray Thomson scattering







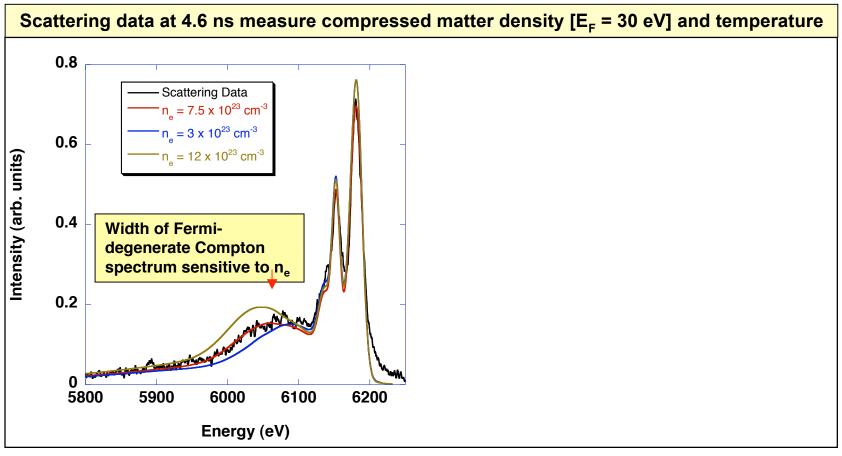
- A new Mn He- α backlighter at 6 keV was applied to penetrate through the dense compressed Be
- Disadvantage: double peaks from He- α and intercombination line





First X-ray Thomson scattering spectrum from compressed matter (Be)

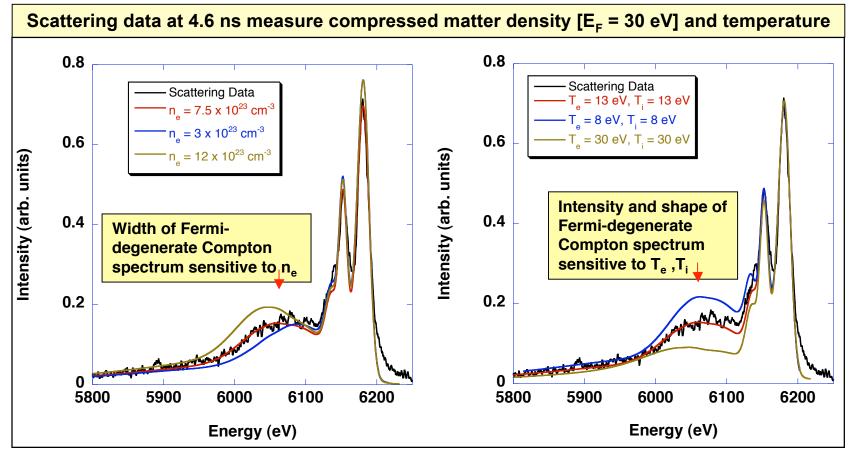






First X-ray Thomson scattering spectrum from compressed matter (Be)



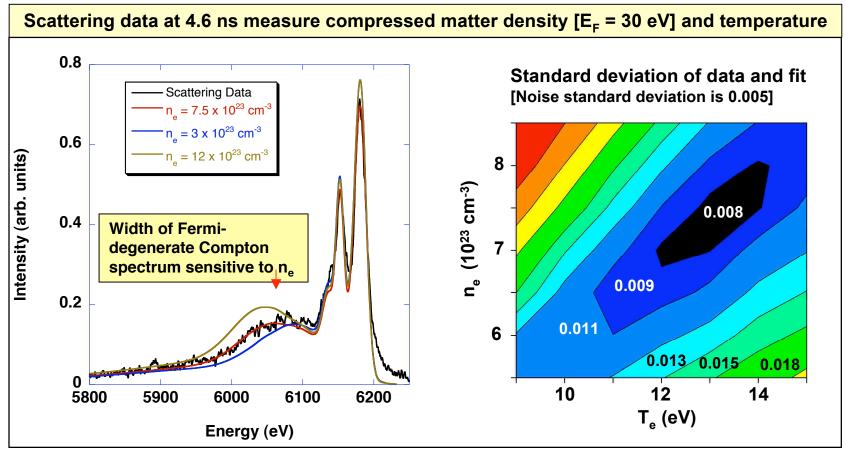


- 90° scatter, non-collective regime: $n_a=7.5\times10^{23}$ cm⁻³, $T_a=13$ eV, Z=2, $\alpha\sim0.5$
- Consistent with simulations and forward scatter results
- First direct measure of increased Fermi energy and adiabat in laser-compressed matter



First X-ray Thomson scattering provides accurate characterization data



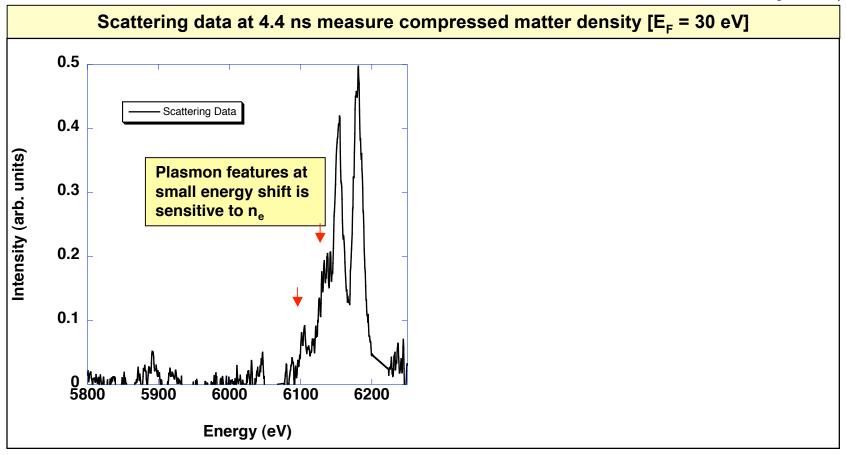


- Density and temperature are determined with an error bar of <10%
- High accuracy due to additional constraints on Z by the forward scattering data



Forward scattering data show plasmons at small energy shifts: collective regime, 25°



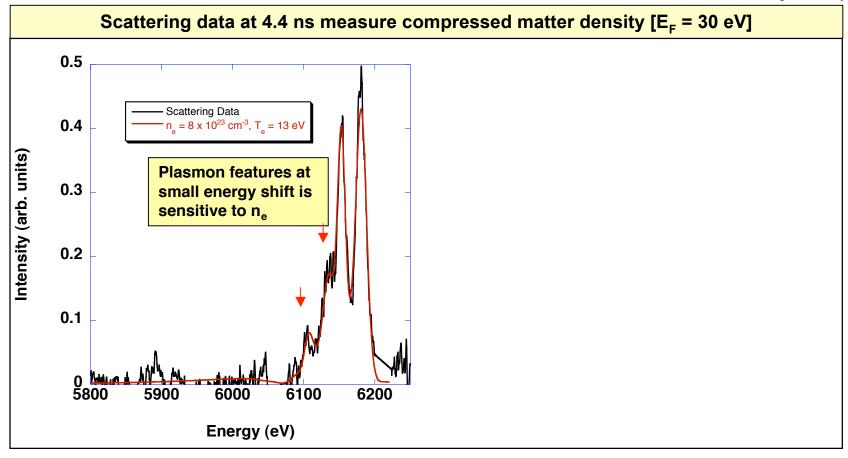


- Forward scatter: $n_e = 7.5 \times 10^{23} \text{ cm}^{-3}$, $T_e = 12 \text{ eV}$, Z = 2, $\alpha \sim 1.6$
- Forward scatter and backscatter results both provide compression of x3
- First direct measure of increased Fermi energy and adiabat in laser-compressed matter



Forward scattering data show plasmons at small energy shifts: collective regime, 25°



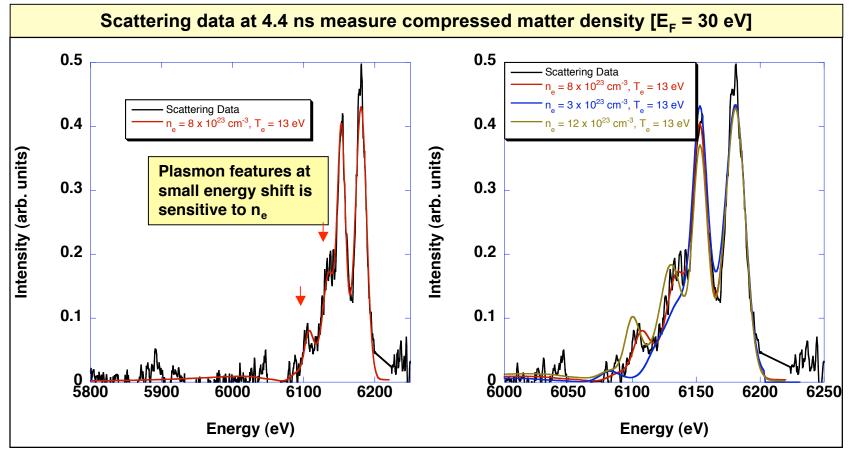


- Forward scatter: $n_e = 7.5 \times 10^{23} \text{ cm}^{-3}$, $T_e = 13 \text{ eV}$, Z = 2, $\alpha \sim 1.6$
- Forward scatter and backscatter results both provide compression of x3
- First direct measure of increased Fermi energy and adiabat in laser-compressed matter



Forward scattering data show plasmons at small energy shifts: collective regime, 25°





- First direct measure of increased Fermi energy, plasmons, and adiabat in laser-compressed matter
- Accurate characterization tool of laser-compressed matter

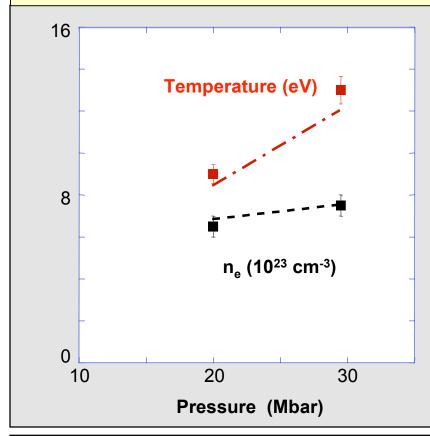




Scattering data will test hydrodynamic simulations of compressed matter conditions



Temperature and density for low and high pressure laser drive



Preliminary comparison with HELIOS calculations (dashed lines) shows that temperature data are critical to test models

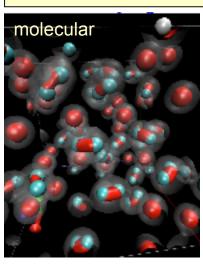
- Electron density is only a weak function of pressure
 - Expected from Be Hugoniot data
- Temperature data
 - Include error from fits only
 - Sensitivity to structure factor calculations S_{ii}(k) is being investigated
 - Experimental tests of structure factors

Structure Factors

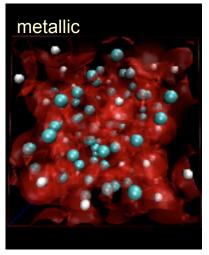
Our experiments have tested the theory of structure factor calculations

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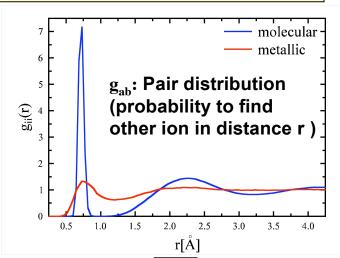
The intensity of the elastic scattering depends on the structure factor - measure for different k: $\left|f_I(k) + q(k)\right|^2 S_{ii}(k,\omega) + ...$

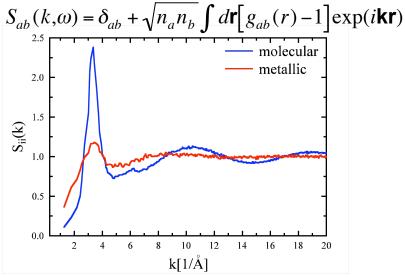


Hydrogen: ρ=0.2 g/cc, T =4000°K



Hydrogen: ρ =3.7 g/cc, T =4000°K



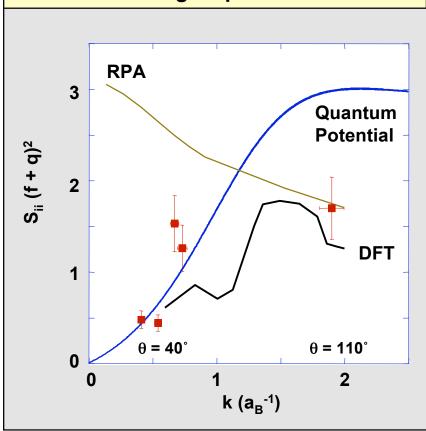


Measurements of the elastic x-ray scattering intensity for varying scattering angles allows testing structure factors



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Ion Structure factor with DFT describes elastic scattering amplitude



$$S(k,\omega) = \left| f_I(k) + q(k) \right|^2 S_{ii}(k,\omega) + \dots$$

Ion feature

Data for

$$- \qquad \mathsf{T_e} = \mathsf{T_i} = \mathsf{12} \; \mathsf{eV}$$

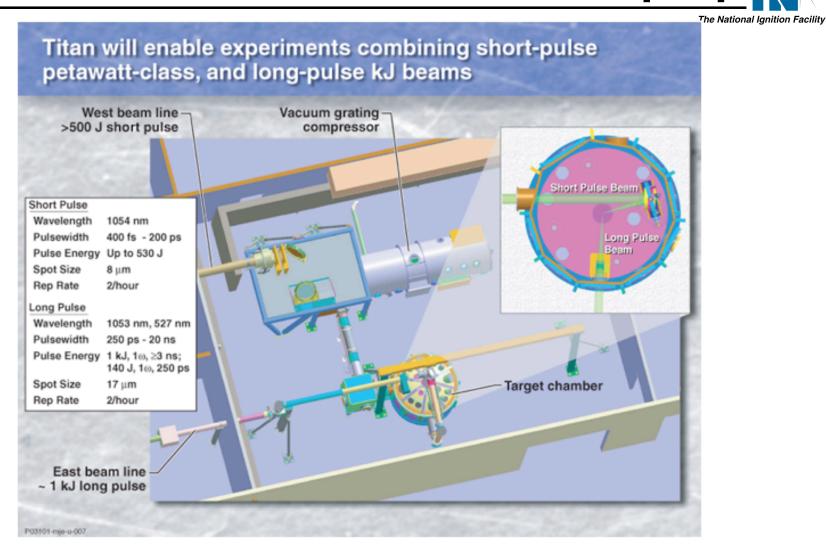
$$n_e = 3 \times 10^{23} \text{ cm}^{-3}$$

- For θ =40° and θ =110° the elastic scattering amplitude is absolutely determined from the inelastic scattering feature
- For k = 2 we have
 - Non-collective scatter
 - q approaches zero
 - S_{ii} approaches one

Density Functional Theory (DFT) has validated weak electron-ion interactions for small k as predicted by quantum potentials

The first inelastic Thomson scattering measurements on a medium-sized laser have been successful on Titan [300 J]





Pump-probe experiments with K-alpha x-rays allowing to probe with 10 ps temporal resolution

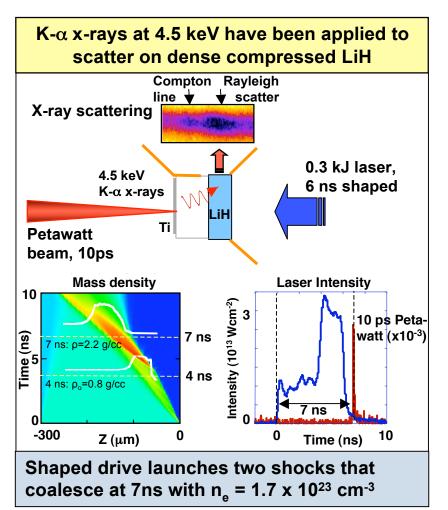
Coalescing shocks

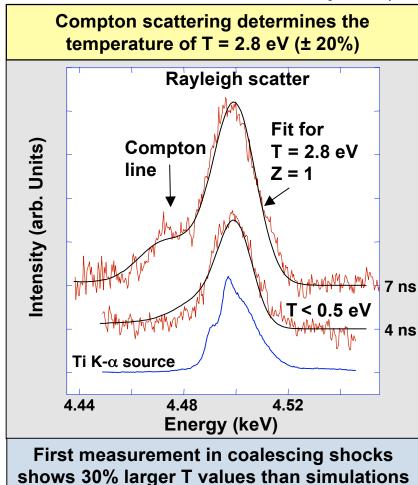


K- α Compton scattering on the LLNL's Titan laser measures temperature in shock-compressed matter with 10 ps resolution



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 Compton scattering on NIF will characterize shock-compressed matter with ultrahigh temporal resolution of 10 ps

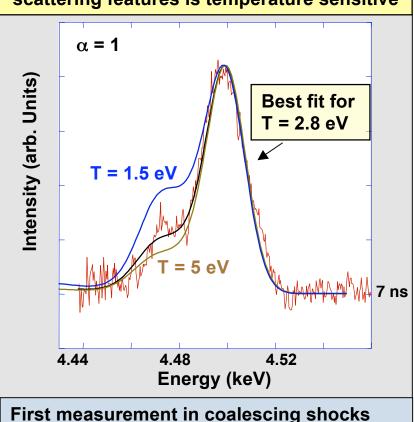




A sensitivity analysis shows that single-shot scattering data determine temperatures with an error bar of 20%



The intensity of the inelastic (Compton) scattering features is temperature sensitive



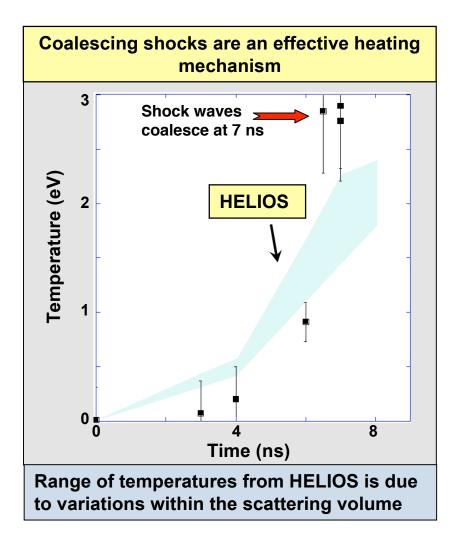
shows T = 2.8 eV (analysis assumes $T_0 = T_i$)

- K-α scattering has been developed to provide accurate characterization of dense matter
- Compressed Matter experiment
 - First successful experiments on compressed LiH
 - Data from Titan are of sufficient quality to test radiation-hydrodynamic modeling
- Density is constraint by the width of the Compton feature
 - Consistent with x 2.8 compression



The Thomson scattering data test hydrodynamic modeling of the temperature evolution in shocked matter





- Temperatures in hydrodynamic modeling is sensitive to
 - Equation of state
 - Radiation transport
 - Heat transport
- Demonstrates technique to characterize NIF Fusion Capsules
 - A sequence of four shocks will have to be accurately timed before compression and burn

X-ray Thomson scattering has been shown to accurately characterize dense compressed matter



- Introduction
 - X-ray Thomson scattering from solid density plasmas
- Proof of principle experiments
 - Backscattering experiment
 - Compton scattering in dense plasmas
 - Accurate temperature diagnostics
 - Forward scattering experiment
 - First observation of Plasmons in Warm Dense Matter
 - Accurate density diagnostic
 - Importance of collisions
- Compressed Matter
 - Compressibility and adiabat
 - Structure Factors
 - Coalescing shocks

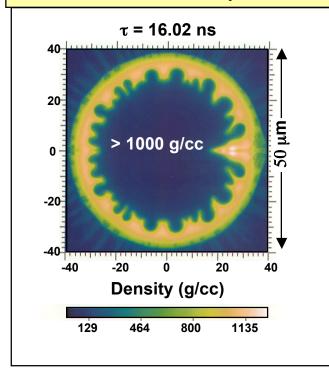
Outlook and Conclusions

Compressed Capsules

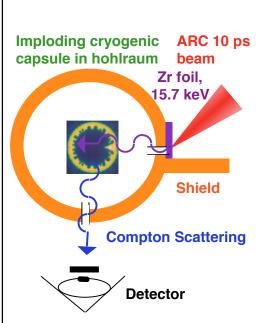
X-ray scattering measures Compton and Plasmon features directly providing T_e/T_F



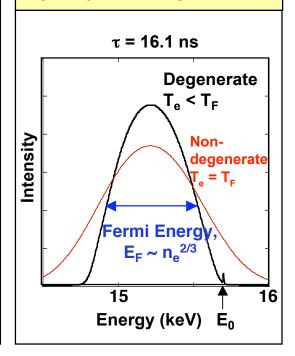
Radiation-hydrodynamic simulations of NIF implosions



Compressed fuel at high density (up to 1000 g/cc), efficient at low T_e : $T_e/T_F < 1$



X-ray scattering spectrum from implosion calculated by post-processing HYDRA



- Goal: Characterize shock-compressed matter
 - Measure temperature and density with ultrahigh temporal resolution
 - Compressibility, demonstrate n_e measurement of up 1000 g/cc

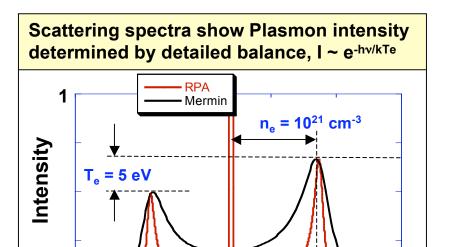




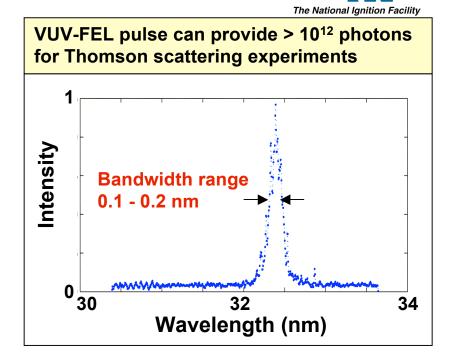
Calculations for Free Electron Lasers indicate accurate characterization of the role of collisions

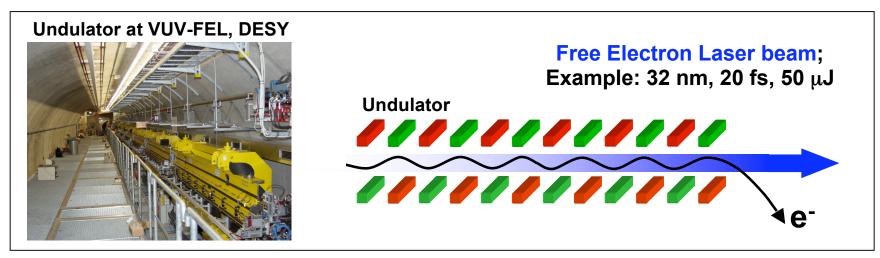
34





Wavelength (nm)





Conclusions



- X-ray Thomson scattering has been developed for accurate measurements of temperatures and densities in dense matter
- Back scatter
 - Measures velocity distribution function: electron temperature T_e
 - Elastic (Rayleigh) scattering:
 Z_{free} diagnostics [n_e in isochorically heated matter]
- Forward scatter
 - First observation of Plasmons in warm dense matter: electron density n_e
 - Future experiments may allow accurate measurement of collisions and conductivity
- Compressed Matter experiments
 - First successful experiments on compressed Be
 - Titan coalescing shocks
 - Technique to characterize NIF Fusion Capsules
 - Technique to characterize high energy density physics regime [equation of state, phase transitions, metallic fluids]

Applications

The first experimental evidence for the Plasma Phase transition have been published this year by Fortov et al.



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The fact that the multiple densities exist for the same pressure would indicate a phase transition; x-ray Thomson scattering can directly determine its existence

